

Time: 3 hours

Max. Marks: 75

Answer any five questions

All questions carry equal marks

1.a) Explain the graphical procedure for solving linear programming problem of two decision variables.

b) Minimize  $z = 2y_1 + 3y_2$  subject to the constraints

$$y_1 + y_2 \geq 5$$

$$y_1 + 2y_2 \geq 6$$

$$y_1 \geq 0, y_2 \geq 0$$

Using big-M method.

[7+8]

2.a) Explain the mathematical formulation of the transportation problem.

b) Determine an initial basic feasible solution for the following transportation problem using North-West corner rule, where  $O_i$  and  $D_j$  represent  $i^{\text{th}}$  origin and  $j^{\text{th}}$  destination respectively.

[7+8]

	D <sub>1</sub>	D <sub>2</sub>	D <sub>3</sub>	D <sub>4</sub>	Supply
O <sub>1</sub>	6	4	1	5	14
O <sub>2</sub>	8	9	2	7	16
O <sub>3</sub>	4	3	6	2	5
Demand	6	10	15	4	35

3.a) Explain the mathematical formulation of Assignment problem.

b) A car hire company has one car at each of five depots a, b, c, d and e. A customer requires a car in each four, namely A, B, C, D, E. Distance (in kms) between depots (origin) and towns (destinations) are given as below.

	a	b	c	d	e
A	160	130	175	190	200
B	135	120	130	160	175
C	140	110	155	170	185
D	50	50	80	80	110
E	55	35	70	80	105

How should the cars be assigned to customers so as to minimize the distance travelled?

[7+8]

4. There are 4 jobs each of which has to go through the machines  $M_1, M_2, M_3, M_4, M_5$  and  $M_6$  in the order  $M_1, M_2, M_3, M_4, M_5$  and  $M_6$ . Processing times are as given below:

Job(j)	Machines (i)					
	M <sub>1</sub>	M <sub>2</sub>	M <sub>3</sub>	M <sub>4</sub>	M <sub>5</sub>	M <sub>6</sub>
A	20	10	9	4	12	27
B	19	8	11	8	10	21
C	13	7	10	7	9	17
D	22	6	5	6	10	14

Determine a sequence of these four jobs which minimize the total collapsed time T. Also find T.

[15]

- 5.a) A truck can carry a total of 10 tons of product. These types of product are available for shipment. Their weights and values are tabulated. Assuming that at least one of each type must be shipped. Determine the loading which will maximize the total value.

Type	Value (Rs)	Weight (tons)
A	20	1
B	50	2
C	60	2

- b) Minimize  $z = 3x + 4y$   
 Subject to  $x \leq 3$ ,  
 $3x + 4y \leq 11$ .

[7+8]

- 6.a) Explain maxi-min and mini-max principle used in game theory with examples.  
 b) Solve the game using dominance.

[8+7]

1	3	4	7
9	5	3	8
10	4	5	6

7. The cost of a machine is Rs 5000. The running cost and the salvage value of the machine are given below. Find when the machine should be replaced.

[15]

Year	1	2	3	4	5	6	7	8
Maintenance cost ( $R_n$ )	1500	1600	1800	2100	2500	2900	3400	4000
Resale price ( $S_n$ )	3500	2500	1700	1200	800	500	500	500

8. A stockist has to supply 400 units of a product every Monday to his customers. He gets the product at Rs.50 per unit from the manufacturer. The cost of ordering and transportation from the manufacturer is Rs.75 per order. The cost of carrying inventory is 7.5% per year of the cost of the product.  
 Find.

- a) The economic lot size.  
 b) The total optimal cost (including the capital cost).  
 c) The total weekly profit if the item is sold for Rs.55 per unit.

[5+5+5]

---ooOoo---