

## Answer any five questions All questions carry equal marks

- 1.a) Explain the complete block diagram of the Digital Control System.
  - b) Define sampling? Mention the advantages, applications and limitations of the sampling in digital control Systems.
- 2.a) Prove Initial Value and Final Value theorems with an example in digital control Systems.
  - b) Obtain the Inverse z-transform for the following using partial fraction method.

$$x(z) = 5/(z-2)(z-4)$$

- c) State the limitations of Z-transform method.
- 3.a) Obtain the z-transform for the following
  - (i)  $f(t) = \sin wt$ .
  - (ii) unit-step function  $\mathbf{u}_{s}(\mathbf{t})$  which is defined as
    - $u_{s}(t) = 1$  t > 0;  $u_{s}(t) = 0$  t < 0
- b) Solve the following difference equation using z-transform method

x(k+2) - 1.5x(k+1) + x(k) = 2 u(k) Where x(0) = 0, x(1) = 1.

4.a) Examine the stability of the following equation using Jury-Stability test.

$$y(k) - 0.4 y(k-1) - 0.61 y(k-2) + 0.87 y(k-3) - 0.22 y(k-4) = x(k)$$

Where x (k) is input and y (k) is output.

b) State the procedure for design of lead compensator using Root-Locus approach.

5.a) Obtain the Pulse Transfer function of the following

$$G(s) = \frac{(1 - e^{-ts})}{s} \frac{1}{s(s+2)}$$

- b) Explain design and derive the Pulse Transfer function of the Digital PD Controller.
- 6.a) For the following equation

 $Y(Z)/U(Z) = (Z+2)/(Z^2+1.2Z+0.2)$ 

Write Controllable Canonical, Observable Canonical and Diagonal Canonical form. b) Consider the discrete-time state equation

$$\begin{bmatrix} x_1(k+1) \\ x_2(k+1) \end{bmatrix} = \begin{bmatrix} 0 & 2 \\ -0.28 & -2 \end{bmatrix} \begin{bmatrix} x_1(k) \\ x_2(k) \end{bmatrix}$$

Obtain the State Transitition Matrix  $\psi$  (k).

Contd....2

7. Consider the following system

x(k+1) = G x(k) + H u(k)

y(k) = C x(k)

Where

 $G = \begin{bmatrix} 0 & -0.32 \\ 2 & -2 \end{bmatrix} \qquad \qquad H = \begin{bmatrix} 0 \\ 1 \end{bmatrix} \qquad C = \begin{bmatrix} 0 & 1 \end{bmatrix}$ 

Design a Full-order State Observer.

8. a) Consider the system defined by

$$\begin{bmatrix} x_1(k+1) \\ x_2(k+1) \end{bmatrix} = \begin{bmatrix} i & j \\ k & l \end{bmatrix} \begin{bmatrix} x_1(k) \\ x_2(k) \end{bmatrix} + \begin{bmatrix} 1 \\ 1 \end{bmatrix} u(k)$$
$$y(k) = \begin{bmatrix} 0 & 1 \end{bmatrix} \begin{bmatrix} x_1(k) \\ x_2(k) \end{bmatrix}$$

Determine the conditions on i, j, k and l for complete state controllability and complete observability.

b) For the following System

 $P(Z) = Z^3 - 1.3Z^2 - 0.08z + 0.24 = 0$ 

Using Bilinear Transformation find the stability of the system.

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