

SIGNALS AND SYSTEMS
 (Common to ECE, EIE, BME, ETM, ICE)

Time: 3 hours

Max. Marks: 75

Answer any five questions
 All questions carry equal marks

- 1.a) Prove that the complex exponential signals are orthogonal functions.
 b) Discuss the properties of Impulse function.
 c) What is orthogonal signal space?
- 2.a) State and prove the time differentiation and time shifting properties of Fourier series.
 b) Obtain the trigonometric Fourier series for the waveform shown below.
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- 3.a) Find the Hilbert transform of $x(t) = \cos \omega_0 t$.
 b) Find the Fourier transform of:
 i) $x(t) = 5 \sin^2(3t)$ ii) $x(t) = 1/(a^2 + t^2)$ iii) $x(t) = \exp(-at) u(t)$.
- 4.a) Obtain the conditions for distortion-less transmission through a system.
 b) Write a note on filter characteristics of linear systems.
- 5.a) Obtain the convolution of the signals $x(t) = \exp(-3t) u(t)$ and $h(t) = u(t+3)$.
 b) Compare ESD and PSD.
- 6.a) Explain the flat top sampling in detail.
 b) Discuss the aliasing and aperture effects and how can they be avoided.
- 7.a) Find the inverse Laplace transform of the following:

$$X(S) = \frac{s^2 + 2s + 5}{(s+3)(s+5)^2}$$

 i) $\text{Re}(S) < -5$ ii) $\text{Re}(S) > -3$ iii) $-5 < \text{Re}(S) < -3$.
 b) Determine the Laplace transform of the signal $x(t) = \sin(\pi t) u(t)$ using periodicity property.
- 8.a) Determine the impulse response of the system described by the difference equation $y(n)-3y(n-1)-4y(n-2) = x(n)+2x(n-1)$.
 b) For the signal $x(n) = -b^n u(-n-1) + (0.5)^n u(n)$. Find the z-transform and plot the ROC.